

## EXPERIMENTAL EVALUATION AND NUMERICAL MODELLING OF THE PRESSURE LOSS THROUGH A COMPRESSOR CASCADE OPERATING AT HIGHLY NEGATIVE INCIDENCE

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### ABSTRACT

The performance prediction of axial flow compressors and turbines still relies on the stationary testing of blade cascades. Most of the blade testing studies are done for operating conditions close to the design point or in off-design areas not too far from it. However, blade – and consequently engine - performance remain unexplored at relatively far off-design conditions (e.g. wind-milling). Such regimes are dominated by blade operation under extremely low mass flows and rotational speeds that imply highly negative values of incidence angle, thus totally separated flows on the pressure side of the blades. Those flow patterns are difficult to be measured and even more difficult to be numerically predicted as the current modelling capability of separated internal flows is of limited reliability. In this paper, the performance of a compressor cascade at highly negative incidence angle (-50 deg. at mid-span) is experimentally investigated. The main objective of the study is to derive the total pressure loss and outlet flow angle through the blades and use the data for the validation-calibration of a numerical solver enhancing its capability to predict highly separated flows. Test rig design details as well the development and calibration of a pneumatic 3- and 5-hole probe are also presented. Flow visualization tests verify the suitability of the designed facility. Finally, numerical results obtained with a commercial CFD solver are compared against the derived experimental data demonstrating a good agreement.

### 1 INTRODUCTION

The experimental verification of any design intent, as far as turbomachinery blading is concerned, is considered to be a very significant step before the integration of a blade design into a gas turbine engine. Traditionally, cascades of blades in linear or annular configuration were employed for the experimental understanding of the complex flow phenomena and the derivation of their performance under various operating conditions (Todd, 1947). A huge range of instrumentation approaches as well as of wind tunnel configurations can be recorded throughout the literature, implying the depth of the experimental studies performed by different research groups (Carter, 1950 and Sieverding, 1985) in this direction. The result of all the extensive studies carried out, especially before the computational revolution, is a large amount of experimental data for different blade families under various conditions, which are currently utilized as a validation platform for more sophisticated predictive methods of numerical or analytical nature (Lieblein, 1965). From a slightly different perspective, analytical expressions derived from experimental data, mainly correlating the pressure loss through the blade channels with the operating conditions, are extensively built into numerical tools, enhancing their reliability-predictability (Lieblein, 1959 and Lieblein, 1956). However, as the major concern of a turbomachinery blade designer is to verify whether a newly designed component performs as it is supposed to do, the majority of the experimental studies carried out, is focused on the design point performance of the blades, while a narrow off-design range of operation is often a topic of research as well (Howell, 1945, Dixon, 1998, Korakianitis, 1993). The latter is reflected in the actual range of the flow incidence angles under which a cascade of blades is experimentally tested which is never wider than +10 -23 degrees in respect to the design point operation that is the operation at zero incidence (Howell, 1942).

In cases that far off-design areas of blade operation are being investigated, additional experimental studies have to be carried out. These usually aim at understanding initially the dominant flow phenomena occurring, and furthermore to describe quantitatively the flow properties such as the pressure change or the deflection angles downstream of the blades. As frequently mentioned within the literature (Kurzke, 1996, Riegler et al., 2000, Alexiou, 2007), multiple benefits can arise from such kinds of studies. Understanding the flow through blades at extremely high incidence enhances the component performance prediction methods but also the whole engine performance simulation for far off-design power settings such as the sub-idle relight transient maneuvers (windmill altitude and quick relights) or groundstarts.

Additionally, the pressure loss modeling can be significantly enhanced with important benefits on the numerical tools where pressure loss models are employed (Novak, 1967, Pachidis et al., 2006). Finally, validation-calibration of CFD codes for predicting the extremely challenging areas of separated flows can be also carried out (Pachidis et al., 2006).

One of the most challenging issues on compressor cascade testing is the accurate and reliable design of the test rig, since compression processes entail implications due to the fact that the flow passages are divergent in area, and thus more instabilities in the flow are expected. This paper describes the design and the calibration of an experimental facility for testing compressor cascades at highly negative incidence angles. Details on the preliminary and also the final design of the rig components, the calibration of each one of them, the overall rig calibration as well as on the selected measuring strategy and the data acquisition system will be presented. A series of flow visualization tests have been carried out in order the effect of the plenum chamber on the periodicity of the flow to be assessed is also presented. The results are compared against CFD predictions of the same flowfield.

The development of the experimental facility for testing compressor blades at high incidence angles (-50 deg. at mid-span) as well as the adopted instrumentation strategy are herein presented as the first but perhaps the most significant parts during the experimental process. A high-quality experimental test, produced on a well designed and calibrated rig, as well as careful choice of the instrumentation set-up increases the confidence on the final measurements, which are particularly complicated under far off-design blade operating conditions. Several other benefits like the validation of numerical tools as well as generation of generic correlations for the description of the off-design performance of turbomachinery blading can also result by such an approach.

## 2 CASCADE GEOMETRY

The compressor cascade under examination consists of nine (9) blades in a linear configuration as shown in Fig. 1. The 3-dimensional blade geometry is described in Fig. 2. A similarity between the incidence angle (Fig. 2 bottom right) and inlet metal angle (Fig. 2 top left) distributions can be easily observed and is due to the fact that the velocity triangle at the inlet of a locked rotor consists only of the axial velocity, thus the incidence angle becomes identical with the inlet metal angle definition. The actual formation of the velocity triangle under those conditions is presented in Fig. 3.

It has been decided the blades to be tested in a linear configuration, instead of an annular one, for two main reasons; (i) the actual blade performance is not the primary objective of this investigation since the experimental work has been set up only for calibration-validation purposes of a correspondent numerical model. The latter is utilized to investigate the annular configuration at a later stage, thus (ii) a relatively easier to be designed and manufactured experimental facility was preferred to avoid the complexity of designing a 3-dimensional wind tunnel to accommodate the blades.

Consequently, the cascade results presented hereafter do not necessarily reflect the actual performance of the blades under the specified conditions and they should be only considered as a calibration-validation platform for numerical models simulating similar phenomena.

### 3 EXPERIMENTAL APPROACH

The experiments were carried out at Cranfield University's low speed cascade wind tunnel designed for testing blades at high incidence. A schematic layout of the facility is presented in Fig 4.

As seen in the picture, the wind tunnel has been design for using in suction mode. Previous wind tunnel designs of different types on which the current configuration is based are given in Gostelow (1984) and Pollard et al. (1967). The bell mouthed intake, installed to smooth the upcoming flow, is followed by boundary layer suction layers just upstream of the blades, eliminating the boundary layer effects in the upstream flow profiles. The boundary layer mass flow is returned at the fan face. The upstream flow uniformity is ensured thanks to a flow straightener installed just after the convergent part of the inlet.

The 9 blade test section comes before a plenum chamber designed to accommodate the outlet flow, aligned with the blade outlet angle at mid span. Preliminary wind tunnel design studies have been carried out using CFD, regarding the definition of the plenum chamber's size and its orientation in order for the wakes to be appropriately accommodated. The main valve for mass flow control is positioned before the additional secondary inlet to ensure that the fan operates far enough from its surge point. Separate valves control both the boundary layer suction flows as well as the secondary fan inlet flow. An image of the experimental facility including the instrumentation mounting as well as the data acquisition system is presented in Fig. 5 and 6 respectively.

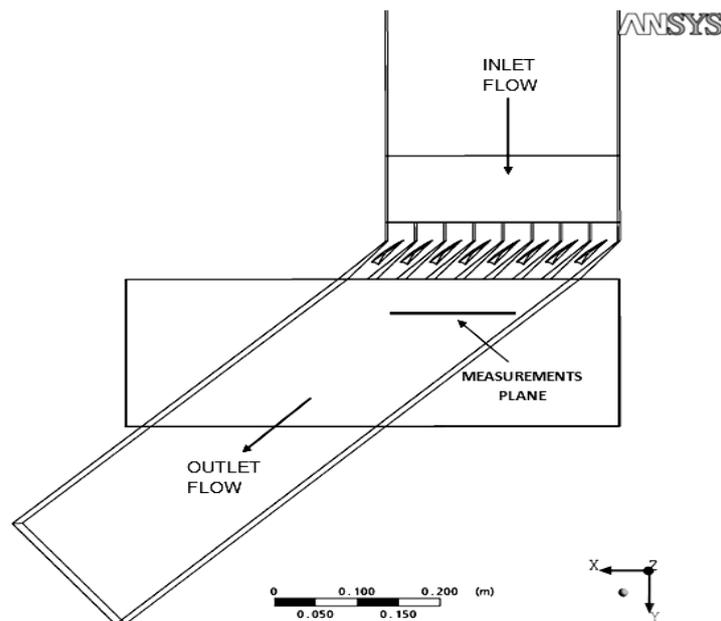


Figure 1 Top view of the compressor cascade domain specifying flow direction and measurement position.

As far as the instrumentation is concerned, a wide variety of methods to choose from is available. As Johansen et al. (2003) mention, steady state flow measurements are typically conducted with pneumatic probes due to their relatively lower response compared to non-intrusive methods (PIV or LDA) typically employed for capturing unsteady flow patterns at high frequencies (Foerster et al., 2000, Schodl, 1975, Wernet et al., 2001). For this study, since the unsteady flow effects were not of primary importance, two pneumatic cobra probes have been employed; a 3-hole probe for a first assessment while a 5-hole probe was used for the higher fidelity final flow field capturing. Both probes were of 2 mm diameter, in-house developed, manufactured and calibrated. The position of the measurement planes was decided to be located at 2 chords downstream of the blades due to the large separation eddies expected within the wakes (see Fig. 1).

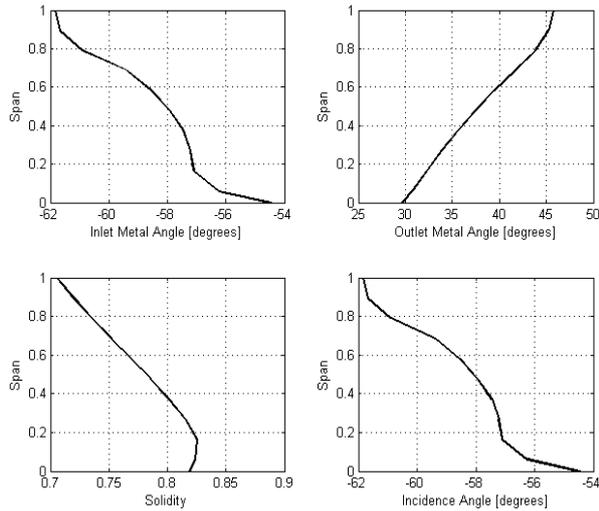


Figure 2 Spanwise distributions of the main blade geometrical features.

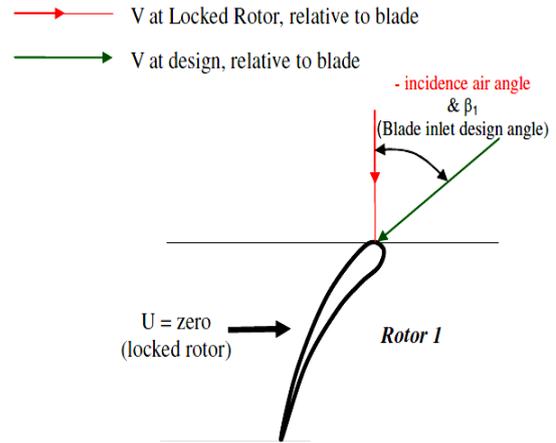


Figure 3 Velocity triangle formulation at locked rotor conditions.

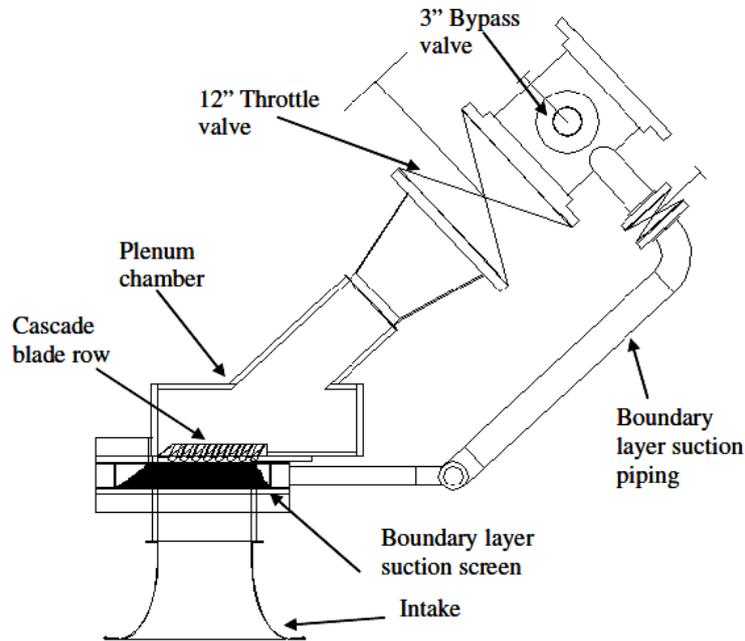


Figure 4 Top view of the experimental facility design.

A fully automated data acquisition interface (hardware and software) was developed for conducting the measurements. A schematic diagram of this system is presented in Fig. 6. The data acquisition system was based on an analogue-to-digital card, with a maximum sampling rate of 20 kHz and a 32-bit resolution. The communication between the A/D card and the PC was achieved employing the DAQ driver software. The data acquisition hardware consists of three transducers, one for each hole of the pneumatic probe. The signal from each transducer is fed into an amplifier module with 'low pass' filters to reject noise frequencies. The three amplified signals are then transmitted to the A/D card in separate channels and finally the measured data is monitored and recorded to files via an interface developed in LabView®.



Figure 5 The experimental facility.

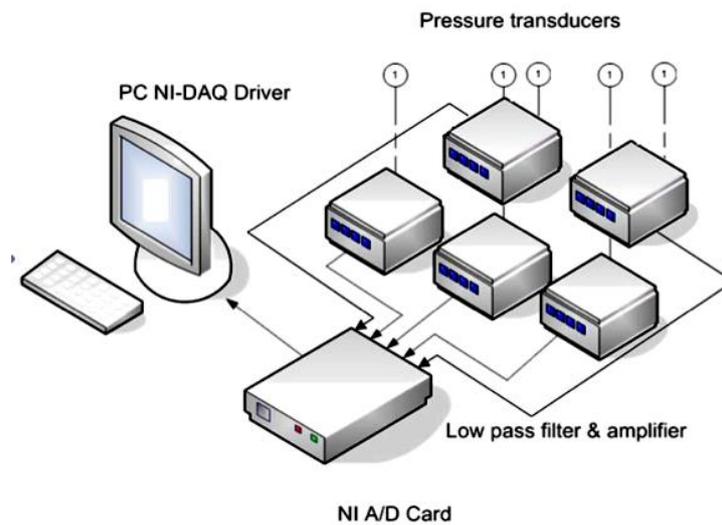


Figure 6 Layout of the data acquisition system.

A LabView® function allows the interpretation of the measured information into the flow properties at each point utilizing the characteristic maps of the pneumatic probe. Therefore, the output information consists of one file for each measurement position downstream of the blades, where the total and static pressure as well as the 3D velocity vector are recorded as a function of time, also dependent upon the acquisition frequency specified as input to the A/D card.

The measurements have been conducted at three different inlet Mach numbers to identify whether there are any Reynolds number effects. The measurement grid consisted of 598 points per channel arranged on a rectangular grid with 23x26 points in the pitchwise and spanwise direction respectively. All the tests were run in a steady state approach averaging the measurements in time. The acquisition frequency was set at 100Hz for a time period of 10 seconds.

At all rig power settings (that is different inlet Mach numbers) the following tests were carried out before conducting the actual measurements in order to ensure the good functionality of the test facility:

- Inlet duct calibration for deriving the actual mass flow and total pressure loss caused by the upstream section.
- Evaluation of the upstream flow profiles.
- Boundary layer suction valve calibration and performance.
- Flow visualisation in the section downstream of the blades to assess the impact of the plenum chamber on the flowfield.
- Tests without blades to assess potential plenum-fan interactions.

It has been established that the flow periodicity downstream of the blades was within an acceptable range, whereas the boundary layer suction valves had to remain at a fully opened position in order to avoid boundary layer growth influence on the upstream flow profiles.

As mentioned above, a number of flow visualization tests in the plenum chamber have been carried out in order for its functionality to be assessed. A fundamental principle that a plenum chamber has to fulfill in order for its design to be considered successful is that the downstream flow must be adequately accommodated without and sidewall effects that may cause pressure gradients in any direction (Gostelow, 1984). In other words the plenum must be large enough to isolate the wall vortex phenomena preventing them from affecting the main downstream flow path that leaves the blade channels. During the development phase of the rig, two main flow visualization test sets carried out; without the blades mounted and with all the blades in place. As shown in the top left side of Fig. 7, in case there are no blades mounted in the rig a single vortex can be observed at the right side of the plenum chamber. A couple of stagnation zones separate the main flow path (that is the stream that leaves the blade channels) from the side wall flow patterns that stay isolated at the right corner. A second, contra-rotating vortex is developed when all the blades are mounted in the test section (see Fig. 7 top right). Due to the presence of the compressor blades, the side wall driven flow region is slightly extended than the previous one with only one stagnation zone this time. In this case, it was found that the blades located closer to this flow area experience a 10-15% lower static pressure than the rest. In other words an undesirable static pressure gradient in the pitch-wise direction downstream of the blades existed. Therefore, a new version of side wall design was triggered by the two first flow visualization tests, with the ambition to eliminate even more the side wall effects and create a uniform static pressure flowfield since it was found that the blades mounted closer to them had an interference with the side vortices of the plenum. The new plenum design is shown in Fig. 7 bottom left. However, the new version of the chamber was no better than the first one as stronger interaction between the blades and the side phenomena was observed. The stream lines of the flow with the revised plenum design are presented in Fig. 7 bottom right. Consequently, the early version of the rig was finally preferred to conduct the experiments. All the final tests were conducted in the middle blade passage to avoid any interaction of the blade flows with the side wall secondary flow patterns.

Finally, the uncertainty within the experimental measurements has been investigated according to the methodology proposed by Abernethy et al. (1985) and adapted by the American Society of Mechanical Engineers (ASME) as a standard uncertainty analysis. The detailed analysis for the 3-hole probe measurements (Zachos et al., 2009a) showed that the total and static pressure as well as the velocity yaw angle values have been measured with an error of 0.0041 kPa, 0.026 kPa and 0.0079 deg respectively. This analysis implies that the most significant uncertainty band is observed at the static pressure derivation whereas the total pressure and the yaw angle lie within extremely narrow uncertainty bands. This can be explained based on the fact that the velocity fluctuations caused by the unsteadiness of the flow are also reflected onto the static pressure flow field while the total pressure remains in much narrower range since it remains unaffected by time dependent phenomena. In addition, the uncertainty analysis conducted for the 5-hole probe acquired data showed that the pressure indications lie within a similar to the 3-hole probe data error band while the pitch angle error is as much as 0.0063 deg.

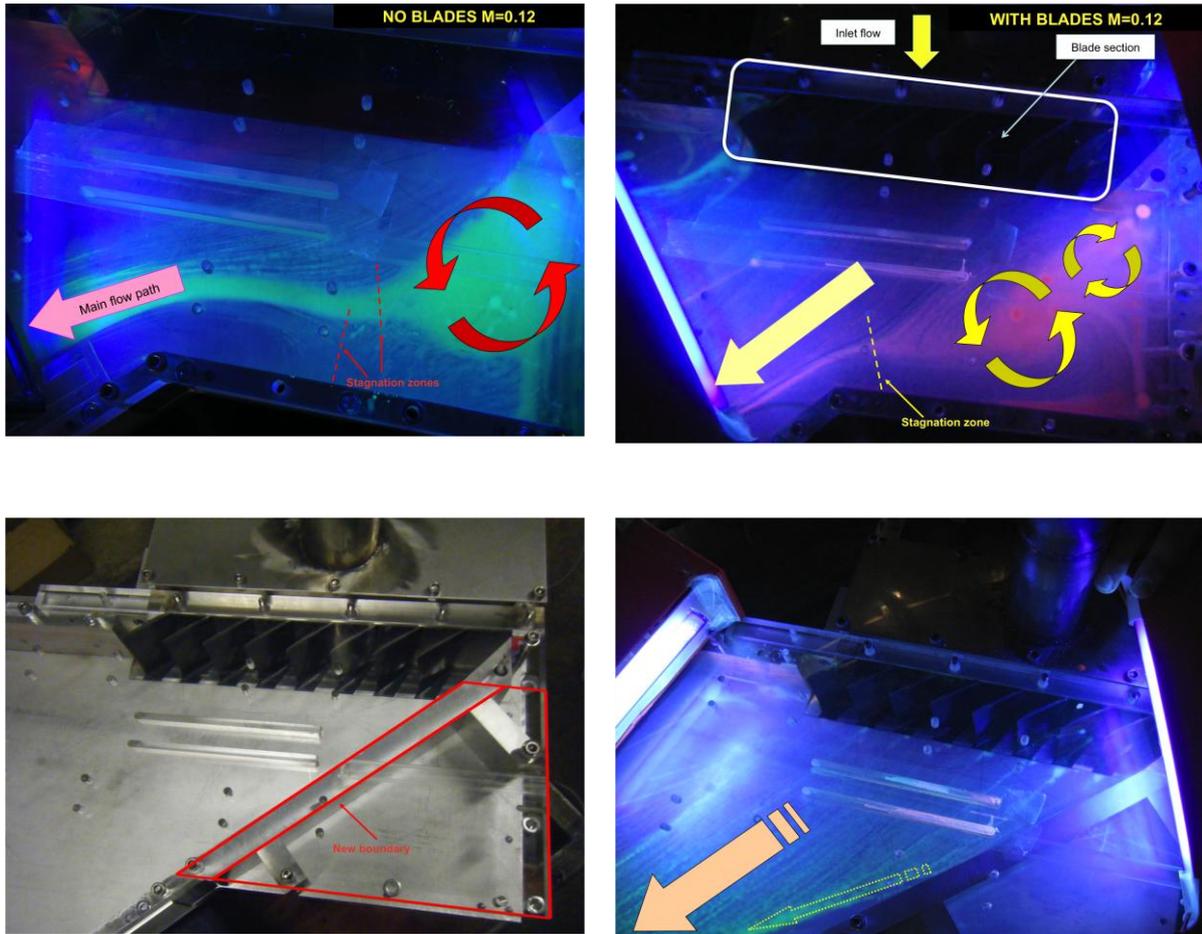


Figure 7 Flow patterns within the plenum the chamber of the rig with no blades mounted (top left), with all the blades in place (top right). New plenum design (bottom left) and stream lines with the new plenum design (bottom right)

#### 4 NUMERICAL APPROACH

The geometrical model used for the numerical calculations is presented in Fig. 8. It consists of an inlet duct, the cascade section, the plenum chamber and an outlet duct. The dimensions of the model reflect the geometry of the experimental facility.

All the numerical simulations of this study have been carried out using ANSYS CFX® solver, widely applied for turbomachinery flow predictions. A high resolution (second order) level of accuracy has been chosen for the solution of the RANS equations.

The computational grid has been separately generated for each one of the above-mentioned domains. All the regions, apart from the boundary layer sectors, have been meshed using hexahedral unstructured approach. The  $y^+$  in every wall has been kept below 20 in such a way that the wall boundary layer could be modeled without employing wall functions. A structured mesh treatment has been employed for the boundary layer sections which was found to be of fundamental importance for predicting the near the wall flow patterns as well as the flow separation. Since the enhanced wall treatment was chosen to be utilized in this study the  $y^+$  had to be kept below 2 in the blade boundary layer regions. The O-mesh configuration employed for the near the wall region in the blade block is illustrated in Fig. 8.

Since one of the most crucial challenges of this numerical study is the robustness of the model and its converging capability, the boundary condition set specified is of great importance. A total pressure at the inlet and a velocity (or mass flow) at the outlet have been applied. Experimental values of the total and

static pressure in the region between the blades and the boundary layer suction block are available from the rig calibration process carried out (Zachos et al., 2009a). Additionally, as the air's density and the upstream area are known, the mass flow can be easily calculated. In general, the total pressure at the inlet is kept constant in all simulations, while the mass flow rate at the outlet is calculated as mentioned above and varies as a function of the inlet Mach number.

A parametric study for the choice of the most suitable turbulence model as well as for the assessment of the uncertainty effects have been carried out and presented in great details by Zachos et al. (2009b). As the analysis of the unsteady effects is not the main objective of this study, no time dependent numerical techniques have been used reducing significantly the computational time with a minimum penalty on the quality of the results.

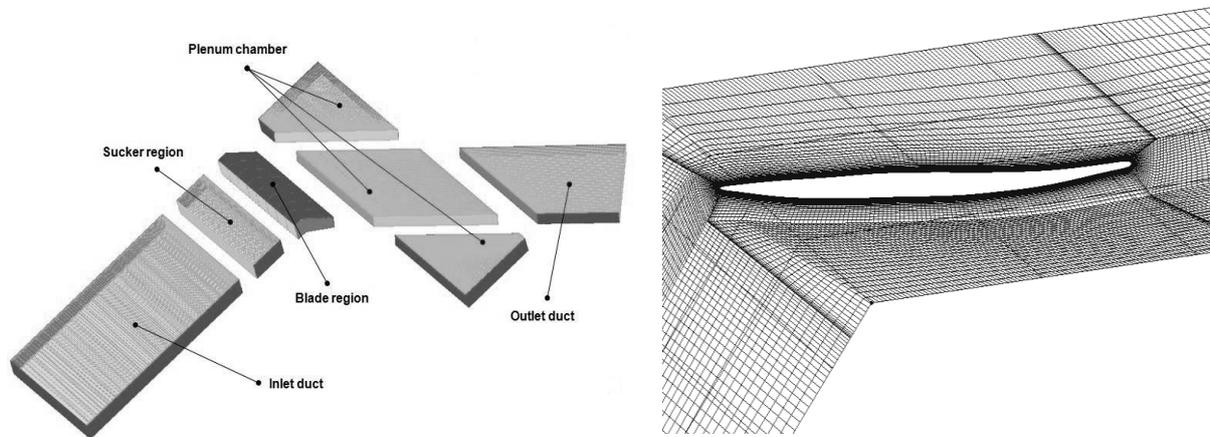


Figure 8 Blocks of the numerical model (left) and O-mesh for the blade boundary layer regions (right).

#### 4 RESULTS AND DISCUSSION

The results of the numerical calculations are presented for the three main inlet Mach numbers, compared against experimental data for validation reasons. For comparing the results on the same basis, the built-in post processor of the numerical solver has not been employed. The flow data is directly exported from the simulation files and is further processed by a separate mass averaging script developed for this reason as described by Greitzer et al. (2004).

As expected, the flowfield is dominated by highly separated flows, as shown in Fig. 10, with a non-reattaching separation region propagating downstream until mixed with similar wakes from the channels nearby.

Comparative plots of the mass averaged total pressure loss, and flow outlet angle in the spanwise direction are presented in Fig. 9 for the three different inlet Mach numbers. As seen, all the pressure loss profiles are in good agreement with the experimental data with the highest deviation at the highest inlet Mach number simulation.

Regions of increased pressure loss can be observed at the hub and the tip, while the presence of the tip leakage vortices looks to affect a higher percentage of the blade span. A uniform pressure loss distribution between 10 – 70% of the blade span can be also highlighted in all cases indicating a less intense interaction of those flow layers with the hub and tip regions of high entropy generation rate.

As far as the comparison against the experimental data is concerned, the biggest deviation seems to exist at the hub region where the boundary layer thickness seems not well predicted by the solver. This happens probably due to the coarse grid definition at the hub region between the blades where most of the secondary flows start from. On the other hand, the tip losses are in good agreement, especially against the 5-hole probe which looks quite capable to capture the 3-dimensional flow phenomena at that region.

Regarding the flow exit angle, the numerical prediction is also in good qualitative agreement with the experimental data following the same trend in all cases with less than 8% deviation from the latter.

The difference in deflection angle can be partially explained using the difference observed in the outlet velocity. For a defined control volume of one blade passage the mass conservation equation must be valid, therefore bigger deflection angles imply lower velocity. Obviously, the channel mass flow is slightly different

between the numerical and experimental approach, however, the total pressure loss remains unaffected, since the results are expressed in a mass averaged format.

As expected, the deflection angle's independency upon the inlet conditions can be also predicted by the solver as illustrated in Fig. 11 where the deflection angle distributions are presented for the entire range of inlet conditions tested.

Regarding the overall cascade performance prediction, the total pressure loss coefficient (defined as the mass-averaged total pressure loss through the blades upon the inlet dynamic head) is presented in Fig. 11 in comparison to the experimental data. As seen from the plot, the weak dependency of the total pressure loss coefficient upon the inlet conditions can be also observed by the numerical results implying the not so strong independency of the flow with the Reynolds number.

In addition, the loss coefficient is slightly under estimated by the numerical tool which may be due to the less losses predicted. As already mentioned, the experimental results have been obtained using a 3- and a 5-hole pneumatic probe. However, regardless of their magnitude, 3-dimensional flow effects exist in any position due to the highly 3-dimensional blade geometry. Thus, due to the limited capability of the instrumentation to capture such phenomena, velocity components not in the yaw or pitch plane cannot be captured by the probes. Therefore, less total pressure downstream of the blades is recorded and consequently an increase in the total pressure loss is observed. and especially in the case of a 3-hole probe measurements.

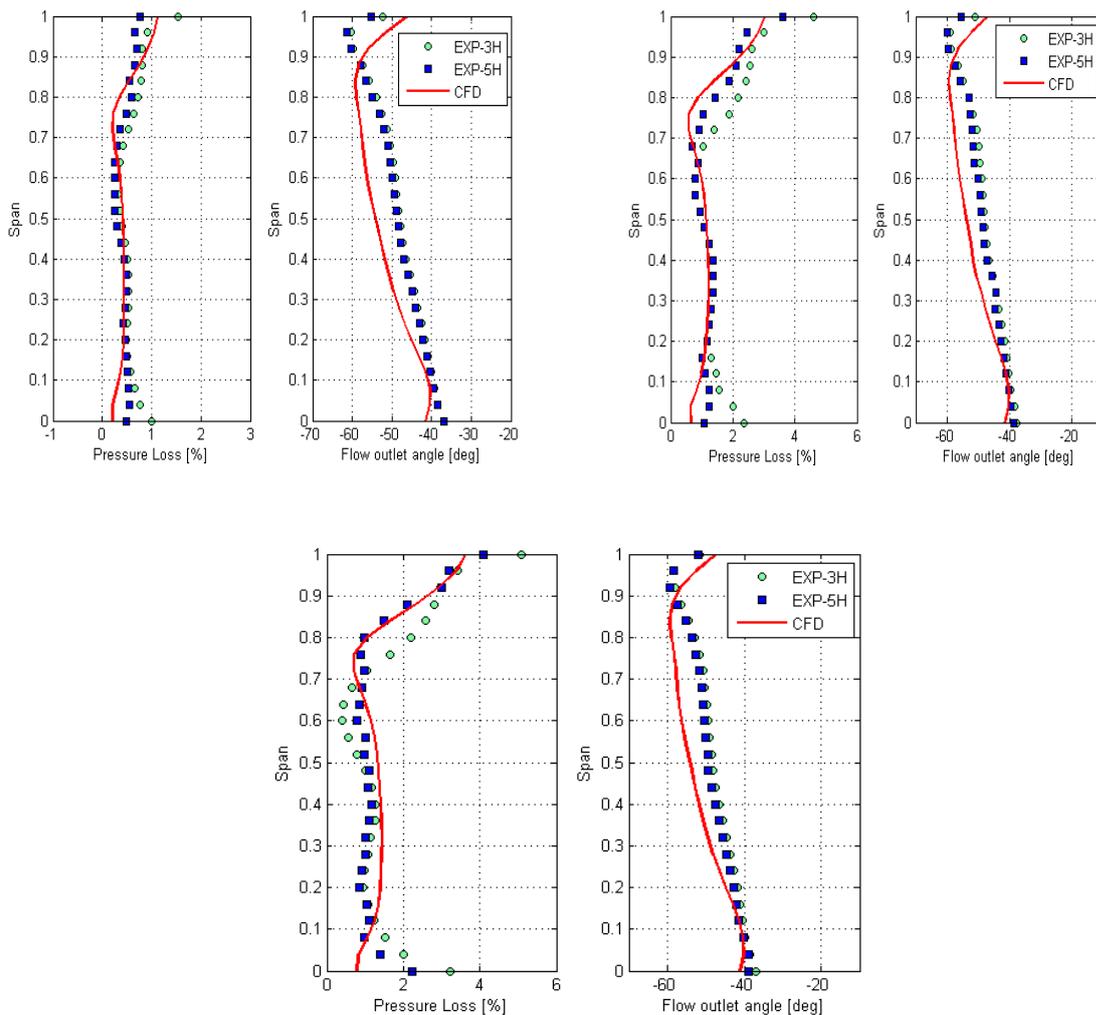


Figure 9 Spanwise loss and outlet angle for M=0.07 (top left) M=0.1 (top right) and M=0.12 (bottom).

On the other hand, as can be also seen by the spanwise distributions of the flow properties, the numerical solver under estimates effects near the bottom wall. Moreover, a poor definition of the computational grid in the hub and top endwalls in the section between the blades results in an additional factor which limits the overall pressure loss in low levels, since the 3-dimensional viscous effects in that

area are not appropriately predicted.

Consequently, the deviation between the measured and predicted total pressure loss for the current cascade is justified. Since it is reasonable the solver to under-estimate the pressure loss while the testing provides with over-estimated loss data, it can be securely claimed that the most realistic value of the overall energy loss is included within the above-defined range of values as defined by the simulation and the experimental results that is between 1.4 and app. 1.45 in overall.

## 5 CONCLUSIONS

In the current work, the flow through a compressor cascade at highly negative incidence angle has been experimentally and numerically investigated. Design details of the test facility, as well as blade geometrical features have been also presented. The test program followed before and during the flow measurements is described. The flow conditions are explained whereas results regarding the total pressure loss through the cascade are presented as a function of the span of the blade for each inlet Mach number tested. The overall cascade properties (total pressure loss coefficient and flow exit angle) are summarized as a function of the inlet flow conditions. A CFD model for predicting the flowfield through the blades has been developed and validated against the experimental data acquired. Details about the meshing strategy, the boundary conditions and the turbulence closure used have been also presented. An assessment of the unsteadiness of the flow has been carried out, which showed that the phenomena are highly periodically. Thus, an unsteady simulation approach is not required if the model is to be validated against overall performance properties such as pressure loss. The spanwise predicted distributions of pressure loss and deflection angle are compared against the experimental results. In addition, the overall cascade performance at high incidence (total pressure loss and total pressure loss coefficient) is presented as a function of the inlet conditions, validated against the experimental values as well.

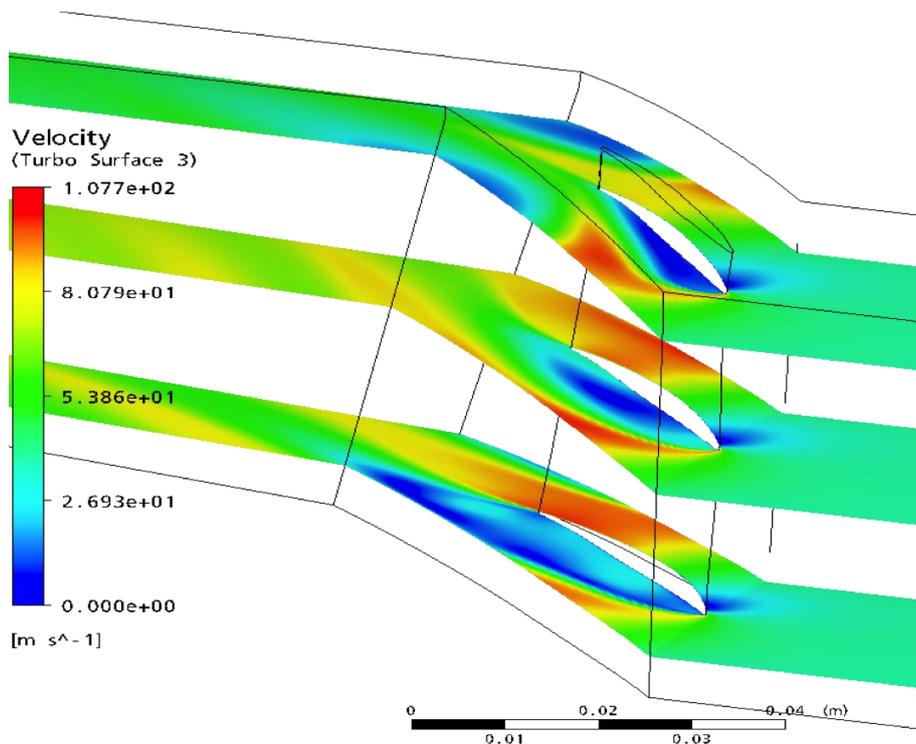


Figure 10 Flow separation structures at different positions along the span.

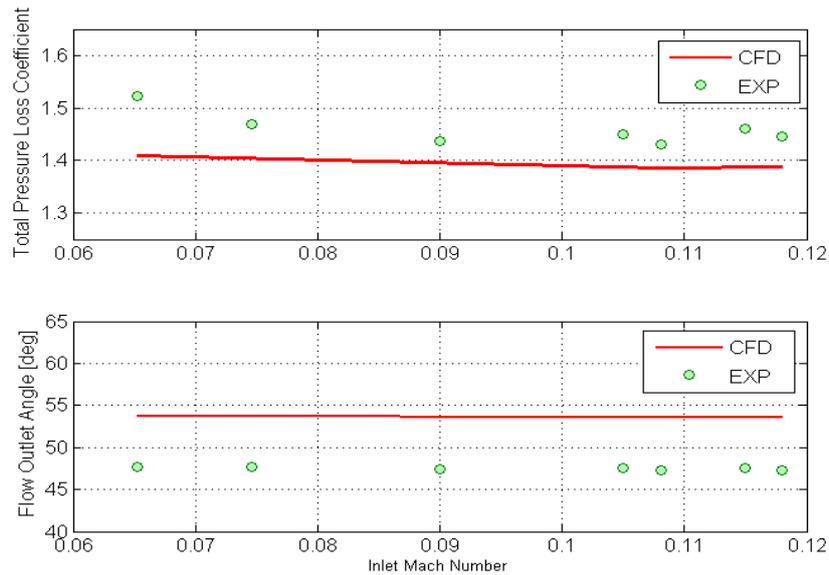


Figure 11 Overall cascade performance as a function of the inlet conditions.

The main conclusions from this study can be summarized as follows:

- The compressor cascade at -58 degrees mid-span incidence angle experiences a total pressure loss coefficient of 1.4– 1.5 weakly dependent upon the inlet flow Mach number.
- The spanwise distributions of the total pressure loss indicate higher losses at the tip of the blade than at the hub region caused by the tip leakage effects.
- The CFD model looks capable enough to capture the flow phenomena struggling only at the hub region. A more complex hub endwall mesh definition may improve the quality of the results in this direction.
- The validation against the experimental data has shown that the pressure loss and deflection angle distributions in the spanwise direction are predicted with less than 8% error. However, considering that this is the first attempt to model so extreme off-design blade operation, the 8% deviation provides confidence for higher accuracy in future similar studies while indicates the challenges for a future numerical prediction of even higher fidelity.
- In overall, the confidence on the highly separated flows prediction is enhanced by the validation against the experimental data, thus numerical models of similar structure can be utilized for further research.

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